

## DAY TWENTY SEVEN

# Unit Test 5

## (Magnetostatics EMI and AC, EM Waves)

- 1 The magnetic field of a given length of wire carrying a current for a single turn circular coil at centre is  $B$ , then its value for two turns for the same wire, when same current is passing through it, is  
(a)  $\frac{B}{4}$  (b)  $\frac{B}{2}$  (c)  $2B$  (d)  $4B$
- 2 A long solenoid carrying a current, produces a magnetic field  $B$  along its axis. If the current is doubled and the number of turns per cm is halved, the new value of the magnetic field is  
(a)  $2B$  (b)  $4B$  (c)  $\frac{B}{2}$  (d)  $B$
- 3 Magnetic field due to 0.1A current flowing through a circular coil of radius 0.1 m and 1000 turns at the centre of the coil is  
(a) 0.2 T (b)  $2 \times 10^{-4}$  T  
(c)  $6.28 \times 10^{-4}$  T (d)  $9.8 \times 10^{-4}$  T
- 4 The magnetic field at a distance  $r$  from a long wire carrying current  $I$  is 0.4 T. The magnetic field at a distance  $2r$ , is  
(a) 0.2 T (b) 0.8 T  
(c) 0.1 T (d) 1.6 T
- 5 A charged particle of charge  $q$  and mass  $m$  enters perpendicularly in a magnetic field  $\mathbf{B}$ . If kinetic energy of the particle is  $E$ , then frequency of rotation is  
(a)  $\frac{qB}{m\pi}$  (b)  $\frac{qB}{2\pi m}$  (c)  $\frac{qBE}{2\pi m}$  (d)  $\frac{qB}{2\pi E}$
- 6 A charge  $q$  moves in a region, where electric field  $\mathbf{E}$  and magnetic field  $\mathbf{B}$  both exist, then the force on it, is  
(a)  $q(\mathbf{v} \times \mathbf{B})$  (b)  $q\mathbf{E} + q(\mathbf{v} \times \mathbf{B})$   
(c)  $q\mathbf{B} + q(\mathbf{B} \times \mathbf{v})$  (d)  $q\mathbf{B} + q(\mathbf{E} \times \mathbf{v})$
- 7 A beam of electrons is moving with constant velocity in a region having simultaneous perpendicular electric and magnetic fields of strength  $20 \text{ Vm}^{-1}$  and 0.5 T, respectively at right angles to the direction of motion of the electrons. Then, the velocity of electrons must be  
(a)  $8 \text{ ms}^{-1}$  (b)  $20 \text{ ms}^{-1}$  (c)  $40 \text{ ms}^{-1}$  (d)  $\frac{1}{40} \text{ ms}^{-1}$
- 8 A straight wire of length 0.5 m and carrying a current of 1.2 A is placed in uniform magnetic field of induction 2 T. The magnetic field is perpendicular to the length of the wire. The force on the wire is  
(a) 2.4 N (b) 1.2 N (c) 3.0 N (d) 2.0 N
- 9 Two wires are held perpendicular to the plane of paper and are 5 m apart. They carry currents of 2.5 A and 5 A in same direction. Then, the magnetic field strength  $\mathbf{B}$  at a point midway between the wires will be  
(a)  $\frac{\mu_0}{4\pi}$  T (b)  $\frac{\mu_0}{2\pi}$  T (c)  $\frac{3\mu_0}{2\pi}$  T (d)  $\frac{3\mu_0}{4\pi}$  T
- 10 An uniform magnetic field acts right angles to the direction of motion of electrons. As a result, the electron moves in a circular path of radius 2 cm. If the speed of electrons is doubled, then the radius of the circular path will be  
(a) 2.0 cm (b) 0.5 cm  
(c) 4.0 cm (d) 1.0 cm
- 11 The work done in turning a magnet of magnetic moment  $M$  by an angle of  $90^\circ$  from the meridian, is  $n$  times the corresponding work done to turn it through an angle of  $60^\circ$ . The value of  $n$  is given by  
(a) 2 (b) 1  
(c) 0.5 (d) 0.25

- 12** Two bar magnets having same geometry with magnetic moments  $M$  and  $2M$ , are firstly placed in such a way that their similar poles are on the same side, then its period of oscillation is  $T_1$ . Now, the polarity of one of the magnets is reversed the time period of oscillations becomes  $T_2$ .

Then,

- (a)  $T_1 < T_2$     (b)  $T_1 > T_2$     (c)  $T_1 = T_2$     (d)  $T_2 = \infty$

- 13** In which type of material, the magnetic susceptibility does not depend on temperature?

- (a) Diamagnetic                      (b) Paramagnetic  
(c) Ferromagnetic                    (d) Ferrite

- 14** A diamagnetic material in a magnetic field moves

- (a) perpendicular to the field  
(b) from weaker to the stronger parts of the field  
(c) from stronger to the weaker parts of the field  
(d) None of the above

- 15** A magnetic field of  $2 \times 10^{-2}$  T acts at right angles to a coil of area  $100 \text{ cm}^2$ , with 50 turns. The average emf induced in the coil is 0.1 V, when it is removed from the field in  $t$  second. The value of  $t$  is

- (a) 10 s    (b) 0.1 s    (c) 0.01 s    (d) 1 s

- 16** A conductor of length 0.4 m is moving with a speed of  $7 \text{ ms}^{-1}$  perpendicular to a magnetic field of intensity  $0.9 \text{ Wbm}^{-2}$ . The induced emf across the conductor is

- (a) 1.26 V    (b) 2.52 V    (c) 5.04 V    (d) 25.2 V

- 17** If the number of turns per unit length of a coil of solenoid is doubled, the self-inductance of the solenoid will

- (a) remain unchanged    (b) be halved  
(c) be doubled    (d) become four times

- 18** A varying current in a coil change from 10 A to zero in 0.5 s. If the average emf induced in the coil is 220 V, the self-inductance of the coil is

- (a) 5 H    (b) 6 H    (c) 11 H    (d) 12 H

- 19** In an inductor of self-inductance  $L = 2 \text{ mH}$ , current changes with time according to relation  $I = t^2 e^{-t}$ . At what time emf is zero?

- (a) 4 s    (b) 3 s    (c) 2 s    (d) 1 s

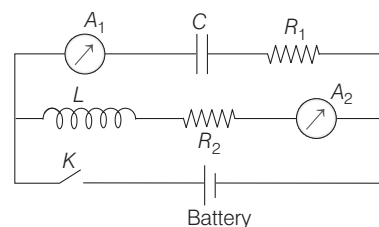
- 20** A 100 mH coil carries a current of 1 A. Energy stored in its magnetic field is

- (a) 0.5 J    (b) 1 A    (c) 0.05 J    (d) 0.1 J

- 21** Two coils have a mutual inductance of 0.005 H. The current changes in the first coil according to equation  $I = I_0 \sin \omega t$ ,  $I_0 = 10 \text{ A}$  and  $\omega = 100 \pi \text{ rads}^{-1}$ . The maximum value of emf in the second coil is

- (a)  $2\pi$     (b)  $5\pi$     (c)  $\pi$     (d)  $4\pi$

- 22** In a circuit inductance  $L$  and capacitance  $C$  are connected as shown in figure.  $A_1$  and  $A_2$  are ammeters. When key  $K$  is pressed to complete the circuit, then just after closing key ( $K$ ), the reading of current will be



- (a) zero in both  $A_1$  and  $A_2$   
(b) maximum in both  $A_1$  and  $A_2$   
(c) zero in  $A_1$  and maximum in  $A_2$   
(d) maximum in  $A_1$  and zero in  $A_2$

- 23** In an experiment, 200 V AC is applied at the ends of an  $L$ - $C$ - $R$  circuit. The current consists of an inductive reactance ( $X_L$ ) = 50  $\Omega$ , capacitive reactance ( $X_C$ ) = 50  $\Omega$  and ohmic resistance ( $R$ ) = 10  $\Omega$ . The impedance of the circuit is

- (a) 10  $\Omega$                                       (b) 20  $\Omega$   
(c) 30  $\Omega$                                       (d) 40  $\Omega$

- 24** The current in self-inductance  $L = 40 \text{ mH}$  is to be increased uniformly from 1 A to 11 A in 4 ms. The emf induced in the inductor during the process, is

- (a) 100 V                                      (b) 0.4 V  
(c) 4.0 V                                      (d) 440 V

- 25** An  $L$ - $C$ - $R$  series circuit is connected to a source of alternating current. At resonance, the applied voltage and the current flowing through the circuit will have a phase difference of

- (a)  $\pi$                                               (b)  $\frac{\pi}{2}$   
(c)  $\frac{\pi}{4}$                                               (d) zero

- 26** A wire of resistance  $R$  is connected in series with an inductor of reactance  $\omega L$ . Then, quality factor of  $R$ - $L$  circuit is

- (a)  $\frac{R}{\omega L}$                                               (b)  $\frac{\omega L}{R}$   
(c)  $\frac{R}{\sqrt{R^2 + \omega^2 L^2}}$                                               (d)  $\frac{\omega L}{\sqrt{R^2 + \omega^2 L^2}}$

- 27** Which of the following combinations should be selected for better tuning of an  $L$ - $C$ - $R$  circuit used for communication?

- (a)  $R = 20 \Omega$ ,  $L = 15 \text{ H}$ ,  $C = 35 \mu\text{F}$   
(b)  $R = 25 \Omega$ ,  $L = 2.5 \text{ H}$ ,  $C = 45 \mu\text{F}$   
(c)  $R = 15 \Omega$ ,  $L = 3.5 \text{ H}$ ,  $C = 30 \mu\text{F}$   
(d)  $R = 25 \Omega$ ,  $L = 15 \text{ H}$ ,  $C = 45 \mu\text{F}$

- 28** For a series  $L$ - $C$ - $R$ -circuit, the power loss at resonance is

- (a)  $\frac{V^2}{\omega L - \frac{1}{\omega C}}$                                               (b)  $I^2 C\omega$   
(c)  $I^2 R$                                               (d)  $\frac{V^2}{\omega C}$

**29** An alternating current generator has an internal resistance  $R_g$  and an internal reactance  $X_g$ . It is used to supply power to a passive load consisting of resistance  $R_L$  and a reactance  $X_L$ . For maximum power to be delivered from the generator to the load, the value of  $X_L$  is equal to  
 (a) zero (b)  $X_g$  (c)  $-X_g$  (d)  $R_g$

**30** The primary winding of transformer has 500 turns, whereas its secondary has 5000 turns. The primary is connected to an AC supply of 20V-50 Hz. The secondary will have an output of  
 (a) 2 V, 5 Hz (b) 200 V, 500 Hz  
 (c) 2 V, 50 Hz (d) 200 V, 50 Hz

**31** If  $\epsilon_0$  and  $\mu_0$  are respectively, the electric permittivity and magnetic permeability of free space,  $\epsilon$  and  $\mu$  are the corresponding quantities in a medium, the index of refraction of the medium is  
 (a)  $\sqrt{\frac{\epsilon_0 \mu_0}{\epsilon \mu}}$  (b)  $\sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}}$  (c)  $\sqrt{\frac{\epsilon_0 \mu}{\epsilon \mu_0}}$  (d)  $\sqrt{\frac{\epsilon}{\epsilon_0}}$

**32** A step-up transformer operates on a 230 V line and supplies current of 2 A to a load. The ratio of the primary and secondary windings is 1 : 25. The current in the primary coil is  
 (a) 15 A (b) 50 A (c) 25 A (d) 12.5 A

**33** Two coil of self inductance  $L_1$  and  $L_2$  are placed clear to each other so that focal flux in one CaCl is completely linked with other. If  $M$  is mutual inductance between them, then  
 (a)  $M = L_1 L_2$  (b)  $M = \frac{L_1}{L_2}$  (c)  $M = \sqrt{L_1 L_2}$  (d)  $M = (L_1 L_2)^2$

**34** An LCR series circuit with  $R = 100 \Omega$  is connected to a 200 V, 500 Hz a.c source when only the capacitance is removed, the current leads the voltage by  $6s$ . When only the inductance is removed, the current leads the voltage by  $60^\circ$ . The current in the circuit is  
 (a) 2 A (b) 7 A (c)  $\frac{\sqrt{3}}{2}$  A (d)  $\frac{2}{\sqrt{3}}$  A

**Direction** (Q. Nos. 35-39) In each of the following questions, a statement of Assertion is given followed by a corresponding statement of Reason just below it. Of the statements mark the correct answer as

- (a) If both Assertion and Reason are true and the Reason is the correct explanation of the Assertion
- (b) If both Assertion and Reason are true but the Reason is not correct explanation of the Assertion
- (c) If Assertion is true but Reason is false
- (d) If both Assertion and Reason are false

**35 Assertion** (A) In an electromagnetic wave, the average energy density of electric field is equal to the average energy density of the magnetic field.

**Reason** (R) Electric and magnetic fields are related as  $E = cB$ .

**36 Assertion** (A) Two parallel wires carrying currents in the same direction, attract each other due to magnetic force between them.

**Reason** (R) They attract each other, if the currents flowing in them are in opposite direction.

**37 Assertion** (A) The torque on the coil is maximum, when coil is suspended in a radial magnetic field.

**Reason** (R) The torque tends to rotate the coil about its own axis.

**38 Assertion** (A) When a magnet is brought near iron nails, only translatory force act on it.

**Reason** (R) The field due to a magnet is generally uniform.

**39 Assertion** (A) Susceptibility is defined as the ratio of intensity of magnetisation  $I$  to magnetic intensity  $H$ .

**Reason** (R) Greater the value of susceptibility, smaller the value of intensity of magnetisation  $I$ .

## ANSWERS

<b>1</b> (d)	<b>2</b> (d)	<b>3</b> (c)	<b>4</b> (a)	<b>5</b> (b)	<b>6</b> (b)	<b>7</b> (c)	<b>8</b> (b)	<b>9</b> (b)	<b>10</b> (c)
<b>11</b> (a)	<b>12</b> (a)	<b>13</b> (a)	<b>14</b> (c)	<b>15</b> (b)	<b>16</b> (b)	<b>17</b> (d)	<b>18</b> (c)	<b>19</b> (c)	<b>20</b> (c)
<b>21</b> (b)	<b>22</b> (d)	<b>23</b> (a)	<b>24</b> (a)	<b>25</b> (d)	<b>26</b> (b)	<b>27</b> (c)	<b>28</b> (c)	<b>29</b> (c)	<b>30</b> (d)
<b>31</b> (b)	<b>32</b> (b)	<b>33</b> (c)	<b>34</b> (a)	<b>35</b> (b)	<b>36</b> (c)	<b>37</b> (b)	<b>38</b> (d)	<b>39</b> (c)	



# Hints and Explanations

- 1** Magnetic field at the centre of circular coil,  $B = \frac{\mu_0 NI}{2r}$ .

**Case I**  $N = 1, L = 2\pi r \Rightarrow r = \frac{L}{2\pi}$

$$\therefore B = \frac{\mu_0 \times 1 \times I}{2r} = \frac{\mu_0 I}{2r}$$

**Case II**  $N = 2, L = 2 \times 2\pi r'$

$$\Rightarrow r' = \frac{L}{4\pi} = \frac{r}{2}$$

$$\therefore B' = \frac{\mu_0 \times 2 \times I}{2r'} = \frac{\mu_0 \times 2I}{2 \times (r/2)} = \frac{4\mu_0 I}{2r} = 4B$$

- 2** For a solenoid,  $B = \mu_0 nI$

where,  $n$  = number of turns per unit length

or  $B \propto nI$   
 $\therefore \frac{B_1}{B_2} = \frac{n_1 I_1}{n_2 I_2}$

Here,  $n_1 = n, n_2 = \frac{n}{2}$ ,

$I_1 = I, I_2 = 2I, B_1 = B$   
 Hence,  $\frac{B}{B_2} = \frac{n}{n/2} \times \frac{I}{2I} = 1$  or  $B_2 = B$

- 3** At the centre of circular coil carrying current, the magnetic field,

$$B = \frac{\mu_0 NI}{2r}$$

Given,  $N = 1000, I = 0.1$  A,  $r = 0.1$  m  
 Substituting the values, we get

$$B = \frac{4 \times 10^{-7} \times 1000 \times 0.1}{2 \times 0.1} = 2\pi \times 10^{-4} = 6.28 \times 10^{-4} \text{ T}$$

- 4** Magnetic field due to a long current carrying wire at distance  $r$ , is given by

$$B = \frac{\mu_0}{4\pi} \cdot \frac{2I}{r} \text{ or } B \propto \frac{1}{r}$$

When  $r$  is doubled, the magnetic field becomes halved i.e. now the magnetic field will be 0.2 T.

- 5** Here, magnetic force = centripetal force

i.e.  $qvB = \frac{mv^2}{r}$

or  $qvB = mr\omega^2$  [ $\because v = r\omega$ ]

or  $\omega = \frac{qB}{m}$

If  $\nu$  is the frequency of rotation, then

$$\omega = 2\pi\nu \Rightarrow \nu = \frac{\omega}{2\pi}$$

$$\therefore \nu = \frac{qB}{2\pi m}$$

- 6** When a charged particle moves in region of  $\mathbf{E} \propto \mathbf{B}$ , then the net force will be  $= F_F + F_B = q\mathbf{E} + q(\mathbf{v} \times \mathbf{B})$

- 7** When  $\mathbf{v}, \mathbf{E}$  and  $\mathbf{B}$  are mutually perpendicular to each other and particle pass undeflected then,

$$qvB = qE \Rightarrow v = \frac{E}{B}$$

Here,  $E = 20 \text{ Vm}^{-1}$  and  $B = 0.5 \text{ T}$

$$\therefore v = \frac{20}{0.5} = 40 \text{ ms}^{-1}$$

- 8** A magnetic force is given by

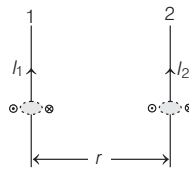
$$F = IlB \sin\theta$$

For  $\theta = 90^\circ$ ,  $F_{\max} = IlB$

Here,  $I = 1.2 \text{ A}, l = 0.5 \text{ m}, B = 2 \text{ T}$

$$F = 2 \times 1.2 \times 0.5 = 1.2 \text{ N}$$

- 9** According to Maxwell's right handed screw rule.



Therefore, net magnetic field

$$B = B_1 - B_2 = \frac{\mu_0 I_1}{2\pi r_1} - \frac{\mu_0 I_2}{2\pi r_2}$$

At mid point,  $r_1 = r_2 = \frac{r}{2} = \frac{5}{2} = 2.5 \text{ cm}$

Hence,

$$B = \frac{\mu_0}{2\pi} \left( \frac{I_1}{r/2} - \frac{I_2}{r/2} \right) = \frac{\mu_0}{2\pi} \left( \frac{5}{2.5} - \frac{2.5}{2.5} \right) = \frac{\mu_0}{2\pi} (2 - 1) = \frac{\mu_0}{2\pi} \text{ T}$$

- 10** The force  $F$  on the charged particle due to magnetic field provides the required centripetal force ( $= mv^2/r$ ) necessary for motion along the circular path of radius  $r$ .

$$\therefore qvB = \frac{mv^2}{r} \text{ or } r = \frac{mv}{qB}$$

$$\therefore r \propto v$$

As,  $v$  is doubled, then the radius also becomes double.

Hence, radius =  $2 \times 2 = 4 \text{ cm}$ .

- 11** Work done in rotating the dipole from

$\theta = \theta_1$  to  $\theta = \theta_2$ , is

$$W = -MB(\cos\theta_2 - \cos\theta_1)$$

**Case I**

$$W_1 = -MB(\cos 90^\circ - \cos 0^\circ) = MB$$

**Case II**  $W_2 = -MB(\cos 60^\circ - \cos 0^\circ)$

$$= -MB\left(\frac{1}{2} - 1\right) = \frac{1}{2}MB = \frac{1}{2}W_1$$

As,  $W_1 = nW_2 \Rightarrow n = 2$

- 12** The time period of bar magnet,

$$T = 2\pi \sqrt{\frac{I}{MH}}$$

When same poles of magnets are placed on same side, then net magnetic moment

$$M_1 = M + 2M = 3M$$

$$\therefore T_1 = 2\pi \sqrt{\frac{I}{M_1 H}} = 2\pi \sqrt{\frac{I}{3MH}} \quad \dots(i)$$

When opposite poles of magnets are placed on same side, then net magnetic moment

$$M_2 = 2M - M = M$$

$$\therefore T_2 = 2\pi \sqrt{\frac{I}{M_2 H}} = 2\pi \sqrt{\frac{I}{MH}} \quad \dots(ii)$$

From Eqs. (i) and (ii), we observe that,  $T_1 < T_2$ .

- 13** For diamagnetic substance, magnetic susceptibility is independent of temperature.

- 14** Diamagnetic substance moves from stronger to weaker field.

- 15** Emf induced in the coil is

$$e = -\frac{d\phi}{dt} = -\frac{(\phi_2 - \phi_1)}{dt}$$

$$\therefore e = -\frac{(0 - NBA)}{dt}$$

$$\text{or } dt = \frac{NBA}{e} = \frac{50 \times 2 \times 10^{-2} \times 10^{-2}}{0.1} = 0.1 \text{ s}$$

- 16** Length of conductor ( $l$ ) = 0.4 m

Speed ( $v$ ) =  $7 \text{ ms}^{-1}$

Magnetic field  $B = 0.9 \text{ Wbm}^{-2}$

Induced emf,  $e = Blv \sin\theta$

$$= 0.9 \times 0.4 \times 7 \times \sin 90^\circ = 2.52 \text{ V}$$

- 17** Self-inductance of solenoid is given by

$$L = \frac{\mu_0 N^2 A}{l}$$

$\therefore L \propto N^2$   
 when  $N$  is doubled,  $L$  becomes 4 times.

- 18** Emf induced in the coil is given by

$$e = -L \frac{dI}{dt}$$

Here,  $dI = I_2 - I_1 = 0 - 10 = -10 \text{ A}$

$$dt = 0.5 \text{ s}, e = 220 \text{ V}$$

$$\therefore 220 = -L \frac{(-10)}{0.5} \text{ or } L = \frac{220}{20} = 11 \text{ H}$$

- 19** It is given that emf is zero i.e.

$$e = -L \frac{dI}{dt} = 0 \text{ or } L \frac{dI}{dt} = 0 \text{ or } \frac{d}{dt}(t^2 e^{-t}) = 0$$

$$\text{or } 2t \times e^{-t} + t^2 \times (-1)e^{-t} = 0$$

$$\text{or } te^{-t}(2 - t) = 0 \Rightarrow t = 2 \text{ s } (\because te^{-t} \neq 0)$$

**20** Energy stored in coil is  $E = \frac{1}{2} LI^2$

where,  $L$  is self-inductance of coil and  $I$  is current induced.

$$\therefore E = \frac{1}{2} \times (100 \times 10^{-3}) \times (1)^2 = 0.05 \text{ J}$$

**21** The given equation of current changing in the first coil is  $I = I_0 \sin \omega t$  ... (i)  
Differentiating Eq. (i) with respect to time, we have

$$\frac{dI}{dt} = \frac{d}{dt}(I_0 \sin \omega t) \text{ or } \frac{dI}{dt} = I_0 \omega \cos \omega t$$

For maximum  $\frac{dI}{dt}$ , the value of  $\cos \omega t$  should be equal to 1.

$$\text{So, } \left(\frac{dI}{dt}\right)_{\max} = I_0 \omega$$

The maximum value of emf is given by

$$\therefore e_{\max} = M \left(\frac{dI}{dt}\right)_{\max} = MI_0 \omega$$

Here,  $M = 0.005 \text{ H}$ ,

$$I_0 = 10 \text{ A}, \omega = 100\pi \text{ rads}^{-1}$$

$$\therefore e_{\max} = 0.005 \times 10 \times 100\pi = 5\pi$$

**22** Initially, there is no DC current in inductive circuit and maximum DC current in capacitive circuit. Hence, the current is zero in  $A_2$  and maximum in  $A_1$ .

**23** Total effective resistance of  $L$ - $C$ - $R$  circuit is

$$Z = \frac{V_0}{I_0} = \sqrt{R^2 + (X_L - X_C)^2}$$

Given,  $V_{AC} = 200 \text{ V}$ ,  $X_L = 50 \Omega$ ,  
 $X_C = 50 \Omega$ ,  $R = 10 \Omega$ ,  $Z = ?$

$$\therefore Z = \sqrt{(10)^2 + (50 - 50)^2} \text{ or } Z = 10 \Omega$$

**24** Emf induced in the coil is given by

$$|e| = L \frac{dI}{dt}$$

$$\therefore |e| = 40 \times 10^{-3} \times \left(\frac{10}{4 \times 10^{-3}}\right) = 100 \text{ V}$$

**25** The impedance ( $Z$ ) of an  $L$ - $C$ - $R$  circuit is given by

$$Z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

At resonance,  $X_L = X_C$

$$\text{i.e. } \omega L = \frac{1}{\omega C}$$

$$\text{As, } \tan \phi = \frac{\omega L - \frac{1}{\omega C}}{R} = 0 \Rightarrow \phi = \text{Zero}$$

So, circuit behaves as, if it contains  $R$  only. So, phase difference = 0

**26** Quality factor =  $Q = \frac{X_L}{R} = \frac{\omega L}{R}$

**27** The  $L$ - $C$ - $R$  circuit used for communication should possess high quality factor ( $Q$  factor) of resonance.

$$\text{which is given by } Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

To make  $Q$  high ;  $R$  should be low ;  $L$  should be high and  $C$  should be low. Therefore, choice (c) is the best suited.

**28** In series  $L$ - $C$ - $R$  circuit at resonance, Capacitive reactance ( $X_C$ )

$$= \text{Inductive reactance } (X_L)$$

$$\text{i.e. } \frac{1}{\omega C} = \omega L$$

Total impedance of the circuit,

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \\ = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$\text{i.e. } Z = R$$

$$\text{So, power factor } \cos \phi = \frac{R}{Z} = \frac{R}{R} = 1$$

Thus, power loss at resonance is given by  $P = V_{\text{rms}} I_{\text{rms}} \cos \phi = V_{\text{rms}} I_{\text{rms}} \times 1$   
 $= (I_{\text{rms}} R) I_{\text{rms}} = (I_{\text{rms}})^2 R = I^2 R$

**29** For delivering maximum power from the generator to the passive load, total reactance must vanish, i.e. or  $X_L = -X_C$ .

**30** The transformation ratio of transformer is given by

$$\frac{V_s}{V_p} = \frac{N_s}{N_p}$$

Making substitution, we obtain

$$V_s = \frac{N_s}{N_p} V_p = \frac{5000}{500} \times 20 = 200 \text{ V}$$

Also, frequency of AC remains unchanged. Thus, option (d) has voltage 200 V and frequency 50 Hz.

**31** Refractive index of medium is given by  $n = c/v$

$$\text{Here, } c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \text{ and } v = \frac{1}{\sqrt{\mu \epsilon}}$$

$$\therefore n = \frac{\sqrt{\mu \epsilon}}{\sqrt{\mu_0 \epsilon_0}} = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}}$$

**32** For a transformer,  $\frac{V_p}{V_s} = \frac{N_p}{N_s}$

Also the power remains constant, if  $\eta = 100\%$

$$\text{So, } V_p I_p = V_s I_s \Rightarrow \frac{I_p}{I_s} = \frac{V_s}{V_p} = \frac{N_s}{N_p}$$

$$\text{Here, } \frac{N_p}{N_s} = \frac{1}{25}, I_s = 2 \text{ A}$$

$$\therefore \frac{I_p}{2} = \frac{25}{1}$$

$$\text{or } I_p = 25 \times 2 = 50 \text{ A}$$

**33**  $M = -\frac{e_2}{di_1/dt} = -\frac{e_1}{di_1/dt}$

$$\text{Also, } e_1 = -L_1 \frac{di_1}{dt} \Rightarrow L_1 = \frac{e_1}{di/dt}$$

$$e_2 = -L_2 \frac{di_2}{dt} \Rightarrow L_2 = \frac{e_2}{di/dt}$$

$$M^2 = \frac{e_1 e_2}{\left(\frac{di}{dt}\right) \left(\frac{di}{dt}\right)} = L_1 L_2 \Rightarrow M = \sqrt{L_1 L_2}$$

**34** If the capacitance is removed, it is an  $L$ - $R$  circuit  $\phi = 60^\circ$ .

$$\tan \phi = \frac{X_L}{R} = \tan 65^\circ = \sqrt{3}$$

If inductance is removed, it is a capacitive circuit or  $R$ - $C$  circuit.  $|\phi|$  is the same

$$\therefore L\omega = \frac{L}{C\omega} \text{ this is resistance circuit.}$$

$$z = R, I_{\text{rms}} = \frac{E_{\text{rms}}}{R} \Rightarrow E_{\text{rms}} = 200 \text{ V}$$

$$I_{\text{rms}} = \frac{200}{100} = 2 \text{ A}$$

**35** Energy density in electric field is

$$U_E = \frac{1}{2} \epsilon_0 E^2$$

Energy density in magnetic field is

$$U_B = \frac{1}{2\mu_0} B^2$$

We know that,

$$E = cB$$

$$\text{and } c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

$$\therefore U_E = \frac{1}{2} \epsilon_0 E^2 = \frac{1}{2} \epsilon_0 (cB)^2 \\ = \frac{1}{2} \epsilon_0 \times \frac{1}{\mu_0 \epsilon_0} \times B^2 = \frac{B^2}{2\mu_0} = U_B$$

Therefore,  $U_E = U_B$

**36** We know that, when two parallel wires carrying currents in same direction attract each other due to magnetic interaction but, if they carry currents in opposite directions, they repel each other.

**37** The torque on the coil is given by  $\tau = nIBA \cos \theta$

When the magnetic field is radial, then coil is set with its plane parallel to magnetic field i.e.  $\theta = 0$ , hence  $\cos \theta = 1$ ,  
 $\tau_{\max} = nIBA \times 1 = nIBA$

**38** The field due to a magnet is non-uniform. Therefore, it exerts both, a net force and a torque on the nails which will translate and also rotate the nails before striking to North pole of magnet with their induced South poles and vice-versa.

**39** From the relation, susceptibility of the material is  $\chi_m = \frac{I}{H} \Rightarrow \chi_m \propto I$

Thus, it is obvious that greater the value of susceptibility of a material greater will be the value of intensity of magnetisation.